Do Recessions Slow Technology Growth? Evidence From the Firm Level

Michaela Elfsbacka-Schmöller¹ Olga Goldfayn-Frank² Tobias Schmidt²

¹European Central Bank and Bank of Finland

²Deutsche Bundesbank

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Finland, Deutsche Bundesbank or the Eurosystem.

MOTIVATION

- Well-established insights from endogenous growth theory (Romer (1990), Aghion and Howitt (1992), Grossman and Helpman (1991))
 - 1. Driver of long-run growth = technology growth.
 - 2. The main determinant of technology growth is investment in innovation.

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- Technology in workhorse models of cyclical fluctuations:
 - Abstract from modeling technology dynamics endogenously in general equilibrium.
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- Technology in workhorse models of cyclical fluctuations:
 - Abstract from modeling technology dynamics endogenously in general equilibrium.
 - $A_t = f(\rho, \epsilon)$, with $\epsilon \sim i.i.d \ N(0, \sigma)$.
- Exogenous technology short-cut implies substantial assumptions:
 - Cyclical fluctuations → innovation, technology and TFP.
 - Business cycles = short-term phenomenon, strict dichotomy between cycle and trend.

This paper

Key question: Do firms cut their investment in innovation in a recession? Insights from previous literature:

- Procyclicality of aggregate innovation and TFP (Barlevy (2007), Fatas (2000)).
- Persistent effects of recessions through drop in technology-enhancing investment
 - Medium-term business cycles (Comin and Gertler (2006))
 - Contractionary demand shocks, innovation and TFP (Jorda et al. (2023), Anzoaetgui et al. (2019))

 $\textbf{Mechanism: contraction} \rightarrow innovation \ investment \downarrow \rightarrow technology \ growth \downarrow$

- Tentative evidence (aggregated data, theory)
- Challenges: identification, data availability

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What we do: Firm-level evidence on the innovation investment patterns in a crisis (novel, granular data set) + persistent effects of short-run shocks (theoretical analysis).

RESULTS

- 1. Link between cyclical downturn and innovation investment at the firm level
 - Large, economically substantial cuts: R&D: 750,000€, diffusion: 954,000€.
 - Innovation investment elasticity: 1% cyclical output drop \rightarrow 0.27% \downarrow (R&D), 0.3% \downarrow (diffusion).
- 2. Identification of underlying driving shocks: key role for demand
 - Cyclical demand fluctuations affect innovation and aggregate supply over at least the medium term.
 - Role of financial frictions (amplification; estimates as a lower bound).
- 3. Persistent, not made-up for fall in innovation investment:
 - Innovation investment fell short of pre-crisis plans also over the medium-term.
 - Investment cuts associated with lower labor productivity growth.

PREVIOUS LITERATURE

Procyclicality of innovation investment: Fatás (2000); Comin and Gertler (2006); Barlevy (2007); Anzoategui et al. (2019).

Empirical evidence on long-run effects in TFP through innovation: Ma and Zimmermann (2023), Jordà et al. (2022), Moran and Queralto (2018), Cloyne et al. (2022), Antolin-Diaz and Surico (2022), Ilzetzki (2022).

Models on cycle-trend interaction through hysteresis in TFP: Benigno and Fornaro (2018), Anzoategui et al. (2019), Bianchi et al. (2019), Moran and Queralto (2018), Garga and Singh (2020), Elfsbacka-Schmöller and Spitzer (2021), Fornaro and Wolf (2023).

Micro evidence on long-run effects from financial constraints: Huber (2018); Duval et al. (2020).

Data

Large, representative sample of firms across sectors and size categories

- Bundesbank Online Panel of Firms: representative monthly survey of firms in Germany
- Innovation module: 5500 firms, 2021Q3
- Full distribution of firms (size, sectors), matches aggregate innovation investment.

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Granular and unique joint firm-level information on:

- Frontier innovation (R&D) and non-frontier innovation (diffusion)
- Identification of crisis-induced adjustment: realized vs. pre-crisis plan
- Reasons for adjustment (\rightarrow shocks)
- Crisis-induced drop in production /business activity
- Firm-level expectations
- Detailed further firm characteristics (general; financing and frictions)

Adjustment patterns of investment in technology

	(1)	(2)
	Planned R&D	Did not plan R&D
	mean	mean
No change, R&D	0.693	0.991
Decreased, R&D	0.245	
Increased, R&D	0.062	0.009
Observations	2629	2182

Adjustment shares (R&D)

ADJUSTMENT PATTERNS OF INVESTMENT IN TECHNOLOGY

	(1) Planned R&D	(2) Did not plan R&D		(1) Planned TD	(2) Did not plan TD
	mean	mean		mean	mean
No change, R&D	0.693	0.991	No change, TD	0.763	0.990
Decreased, R&D	0.245		Decreased, TD	0.191	
Increased, R&D	0.062	0.009	Increased, TD	0.046	0.010
Observations	2629	2182	Observations	2934	1846

Adjustment shares (R&D)

Adjustment shares (TD)

- Substantial downward adjustment, mean cuts: -750' €(R&D), -954' €(TD).
- Increases negligible in terms of shares and magnitude (179'€(R&D), 144' €(TD)).
- Average adjustment in R&D -9% closely matches aggregate decline (-6.3% BERD vs. 4% pre-crisis growth).

DOWNWARD ADJUSTMENT RELATIVE TO PLANS

	p10	p50	p75	p90	mean	count
R&D investment: '000 planned	5	50	200	1200	1952	2629
Decrease R&D, % planned amounts	25	67	93	100	65	644

Plans and downward adjustment in R&D, conditional on having plans, by innovator type.

	p10	p50	p75	p90	mean	count
TD investment: '000 euro planned	5	40	200	1000	2049	2932
Decrease TD, % planned amounts	25	71	100	100	69	559

Plans and downward adjustment in TA, conditional on having plans, by innovator type.

INNOVATION ELASTICITY TO CYCLICAL OUTPUT SHIFTS

	R&D investment cuts (pct.)				Diffusion investment cuts (pct.)			
	1	2	3	4	5	6	7	8
Crisis-induced production/ activity drop (0-1)	15.745*** (5.310)	15.256*** (4.994)			11.852** (5.146)	10.639** (5.025)		
Crisis-induced production/ activity drop (pct.)			0.271*** (0.078)	0.275*** (0.077)			0.309*** (0.073)	0.338*** (0.076)
Covariates	No	Yes	No	Yes	No	Yes	No	Yes
Observations	166	166	157	157	153	153	146	146

Elasticities: R&D and diffusion.

REASONS FOR NON-ADJUSTMENT



Conditional on having plans to invest in R&D or TA. Source: BOP-F, Waves 6-8; trimmed data; own calculations.

- 46% did not experience a sufficiently strong change in own economic conditions which would have necessitated adjustment.
- Sufficient financial resources (despite changed situation at the firm-level) prevented further adjustment (33%).
- For a small fraction of firms adjustment was not feasible ("sticky" investment).
- Episode as a lower bound for response during a crisis; importance of fiscal and monetary support.

DEMAND SHOCKS AS KEY DRIVERS OF INNOVATION CUTS



- R&D and diffusion driven by similar shocks (Comin and Gertler (2006)) mechanism
- Key shocks: uncertainty and <u>demand</u>
- Supply-chain disruptions → innovation investment↓ (Fornaro and Wolf (2023))
- COVID policy restrictions contributed *negatively* →→ "innovating out of pandemic"
- Non-binding financial frictions (policy support; non-financial shock)

DEMAND SHOCK AND FINANCIAL FRICTIONS

- 2008/09: procyclical slowdown in TFP growth → relative role of financial shock + frictions and the role of weak demand?
- We show: demand shocks can slow innovation investment and thus long-term aggregate supply even <u>without</u> financial frictions.
- Amplification in the absence of large-scale policy support.
- Amplification under simultaneous demand shock and binding financial constraints (higher share of decreasers; model).



THE ROLE OF EXPECTATIONS: DEMAND AND FINANCIAL CONSTRAINTS

	Prob	Probability to decrease investment					
	R	۷D	Diffusion				
Expect demand problems	0.101***	0.075***	0.076***	0.058***			
	(0.019)	(0.020)	(0.019)	(0.020)			
Expect financing problems	0.059**	0.056**	0.052*	0.060**			
	(0.027)	(0.027)	(0.027)	(0.027)			
Expect problems due to covid restrictions	-0.006	0.007	0.020	0.028			
	(0.027)	(0.027)	(0.020)	(0.019)			
Covariates	No	Yes	No	Yes			
N observations	1300	1293	1278	1271			

Decreased investment in R&D, effect of crisis-induced production drop and expectations

Appendix

The Persistent Effects of Demand Shocks

New Keynesian DSGE model with endogenous growth:

- Horizontal innovation via expanding intermediate good varieties (Romer (1990))
- Two-stage technology growth process (Comin and Gertler (2006):
 - 1. R&D sector: technological frontier
 - 2. Endogenous diffusion of new technologies.
- Medium-scale DSGE framework



Macroeconomic dynamics under a contractionary demand shock

INVESTMENT REMAINED PERSISTENTLY BELOW PRE-CRISIS PLANS

	R&	۷D	т	A
2021 vs. pre-crisis plan 2022 vs. pre-crisis plan	-283.82	-199.38	-918.46	-942.41
Obs.	1478	1468	1436	1435

Comparison of R&D and TA against pre-crisis plan; reported in mean changes, in 1000 euros.

- Innovation cuts not made up for.
- Qualitative drivers of innovation post-2020:
 - Postponed investment/ make-up < 5% of firms.</p>
 - Business cycle factors and long-term planning predominant.
- Innovation investment cuts associated with lower labor productivity growth.

DRIVERS OF FIRMS' INNOVATION INVESTMENT BEYOND 2020



Firms' innovation decision 2021-2022, evidence on underlying drivers.

LABOR PRODUCTIVITY

	Labor productivity growth, 2022/2019					
High R&D cut	-10.024 (12.307)	-1.695 (13.470)				
Covariates N	no 329	yes 327				

Labor productivity growth, 2022 vs. 2019, in %. Firms which had plans and cut investment; high cut defined as above median % change relative to pre-crisis plans.

• Preliminary results, more detailed analysis in progress.

CONCLUSION

- Micro evidence shows that firms cut investment in technology in a recession
 - Fall in both frontier and non-frontier innovation investment \rightarrow persistent slowdown in technology growth.
 - Economically substantial cuts (65%/70% of pre-crisis plans).
 - Cyclical innovation elasticity: 1% cyclical output drop \rightarrow 0.27% \downarrow (R&D), 0.3% \downarrow (diffusion).
- Firm-level evidence of spillovers from short-run fluctuations, in particular via demand shocks, to aggregate supply over at least the medium term.
- Implications for macroeconomic modeling and policy
 - Persistent effects of recession and extended role of stabilization policies.
 - Strict dichotomy between models of cyclical fluctuations and long-term growth?
 - Implications for underlying concepts: cycle vs. trend, potential output, output gap.

Additional slides

QUESTIONNAIRE: PRE-CRISIS INVESTMENT PLANS

Definition for innovation activities (R&D, other innovation)

In the following section, we would like to ask you some questions on the topic of innovations. Innovations are new or improved products or business processes (or a combination thereof) that differ substantially from prior products or business processes and that the enterprise in question has introduced to the market or utilised itself. Innovations are often divided into research and development (R&D) and other innovations.

Question: Think back to the end of 2019, i.e. to the time before the COVID-19 pandemic. How much did you plan to spend on R&D activities and other innovation activities (excluding R&D)?

Note: If you had no expenditure planned for one of the areas, please enter "0".

- Planned expenditure for R&D activities in 2020 amounted to:'000 euro
- Planned expenditure for other innovation activities in 2020 amounted to:'000 euro

Question: How much did your enterpriseise actually spend on R&D activities, other innovation activities (excluding R&D)?

Note: If you had no expenditure in one of the areas, please enter "0".

- Actual expenditure for R&D activities in 2020 amounted to:....'000 euro
- Actual expenditure for other innovation activities in 2020 amounted to:....'000 euro

QUESTIONNAIRE: REASONS FOR NON-ADJUSTMENT

Question: You stated that your firm did not adjust its plans regarding expenditure on R&D or other innovation activities in 2020. Which of the following reasons were the most important?

- We would have reduced investment in innovation, but were not able to make adjustments.
- We would have increased investment in innovation, but were not able to make adjustments.
- Overall, the situation for my firm did not change significantly in 2020.
- We had sufficient financial resources.
- Other reasons.

Non-adjustment

QUESTIONNAIRE: REASONS FOR CHANGE

Question: Which of the following changes linked to the coronavirus pandemic induced an adjustment of your plans regarding expenditure for R&D activities and other innovation activities (excluding R&D) in 2020?

Firms select separately for R&D and other innovation activities.

- More uncertain economic outlook
- Lower/ higher customer demand for existing products and services
- Worse/ better access to intermediate inputs
- Worse/ better availability of suitable specialist staff
- Worse/ better access to financing sources
- Closures or work restrictions due to the coronavirus pandemic (hygiene rules, lockdown etc.)
- Other reasons linked to the coronavirus pandemic
- Reasons not linked to the coronavirus pandemic

Question: The previous questions referred to research and development (R&D) specifically in 2020. What is the situation more generally, does your firm invest in research and development (R&D)?

- Yes, continuously with a specific R&D budget.
- Yes, continuously without a specific R&D budget.
- Yes, occasionally.
- No.

PLANS AND ADJUSTMENT IN AMOUNTS

	p10	p50	p90	mean	count
R&D investment: '000 planned	5	50	1200	1952	2629
Decrease R&D, '000 euro	-700	-30	-5	-750	644
Increase R&D, '000 euro	5	33	338	179	162
Change in R&D, '000 euro	-50	0	0	-173	2629
Change III Roed, 000 euro	-50	0	0	-175	2029

Investment in R&D, '000 euro

	p10	p50	p90	mean	count
TA investment: '000 planned	5	40	1000	2049	2932
Decrease TD, '000 euro	-650	-30	-4	-954	559
Increase TD, '000 euro	5	20	225	144	135
Change in TD, '000 euro	-25	0	0	-175	2932

Investment in TD, '000 euro

- Economically substantial downward adjustment
- Increases negligible both in shares (\sim 5%) and magnitude
- Average adjustment in R&D -9% (aggregate decline:
 - -6.3% BERD vs. 4%

pre-crisis growth)

R&D (dec.)

TD (dec.)

MACROECONOMIC DYNAMICS: BUSINESS R&D



Real GDP (Germany, source: FRED)

Business R&D (Germany, source: FRED)

EXPECTATIONS ABOUT DEMAND



NO SYSTEMATIC DOWNWARD REVISIONS OUTSIDE CRISIS EPISODE



Pre-crisis trends in planned (red line) vs. actually realized innovation expenditures (blue line) in Germany; source: Mannheim Innovation Panel (ZEW); units: bn. euros.

JOINT ADJUSTMENT PATTERNS IN R&D AND TECHNOLOGY DIFFUSION

	(1)	(2)	(3)
	Increased TD	Decreased TD	No change TD
Increased R&D	1.56	1.19	3.25
Decreased R&D	1.19	14.68	9.52
No change R&D	3.93	2.10	60.98

Source: BOP-F, Waves 6-8; trimmed data; own calculations; conditional on having plans to invest in both R&D and T&A.

ADJUSTMENT BY FIRM SIZE AND SECTOR



Downward adjustment by sectors and firm size

Notes: Conditional on having plans to invest in R&D or TA; source: FDSZ der Deutschen Bundesbank, BOP-F, Waves 6-8; own calculations.

- Relatively similar relative decrease in services vs. manufacturing
 - Role of relative output drop
 - Larger plans in *M* for R&D, difference less pronounced in TD
- Downward adjustment more pronounced in small firms vs. large firms
 - Role of financial constraints
 - Larger firms with larger plans

Sect. adj.

Distr.

ADJUSTMENT PATTERNS OF INVESTMENT IN TECHNOLOGY: SHARES (CORE INNOVATORS)

	Planr	ned R&D	No R&D planne		
	core non-core		core	non-core	
	(1)	(2)	(3)	(4)	
No change, R&D	0.664	0.729	0.946	0.994	
Increased, R&D	0.077	0.043		0.006	
Decreased, R&D	0.259	0.228			
Observations	1455	1171	148	2028	

TABLE: Adjustment (shares) in R&D

	Plan	ined TA	Νο ΤΑ	A planned
	core	non-core	core	non-core
	(1)	(2)	(3)	(4)
No change, TA	0.732	0.787	0.985	1.000
Increased, TA	0.054	0.040		
Decreased, TA	0.214	0.173		
Observations	1296	1634	259	1582

TABLE: Adjustment (shares) in TA

Source: BOP-F, Waves 6-8; trimmed data; own calculations.

Main

Firms by investment behavior in R&D - weighted

	(1)	(2)
	Invest in RD continuously	Do not invest in RD continuously
	mean	mean
Invest continuously with budget	0.224	
Invest continuously w/o budget	0.776	
Invest occasionally		0.319
Do not invest typically		0.681
Observations	1817	3671

Source: BOP-F, Waves 6-8; trimmed data; own calculations.

FIRMS BY INVESTMENT BEHAVIOR IN R&D

	(1)	(2)
	Invest in R&D continuously	Invest in R&D occasionally
	mean	mean
Invest continuously with budget	0.286	
Invest continuously w/o budget	0.714	
Invest occasionally		0.358
Do not invest typically		0.642
Observations	1818	3672

Source: BOP-F, Waves 6-8; trimmed data; own calculations.

Adjustment in amounts: R&D (decomposition)

			(1)					(2)		
			All				Cor	re innov	ators	
	p10	p50	p90	mean	count	p10	p50	p90	mean	count
R&D investments: '000 planned	5	50	1200	1952	2629	10	100	3000	3083	1455
Decrease R&D, '000 euro	-700	-30	-5	-750	644	-1000	-50	-7	-966	377
Increase R&D, '000 euro	5	33	338	179	162	5	50	499	174	112
Change in R&D, '000 euro	-50	0	0	-173	2629	-100	0	0	-237	1455

Investment in R&D, conditional on having plans, by innovator type, '000 euro

Amounts

Adjustment in amounts: Diffusion (decomposition)

			(1)					(2)		
			All				Co	re innov	ators	
	p10	p50	p90	mean	count	p10	p50	p90	mean	count
TA investments: '000 planned	5	40	1000	2049	2932	10	80	2000	2581	1295
Decrease TA, '000 euro	-650	-30	-4	-954	559	-1000	-50	-5	-1687	276
Increase TA, '000 euro	5	20	225	144	135	5	50	390	199	70
Change in TA, '000 euro	-25	0	0	-175	2932	-50	0	0	-349	1295

Investment in TD, conditional on having plans, by innovator type, '000 euro

Amounts

DOWNWARD ADJUSTMENT RELATIVE TO PLANS (DECOMPOSITION)

				(1)						(2)		
				All					Core	innovat	ors	
	p10	p50	p75	p90	mean	count	p10	p50	p75	p90	mean	count
R&D investments: '000 planned	5	50	200	1200	1952	2629	10	100	500	3000	3083	1455
Decrease R&D, % planned amounts	25	67	93	100	65	644	20	56	80	100	57	377

TABLE: Plans and downward adjustment in R&D, conditional on having plans, by innovator type

				(1)						(2)		
				All					Core	innovate	ors	
	p10	p50	p75	p90	mean	count	p10	p50	p75	p90	mean	count
TA investments: '000 euro planned	5	40	200	1000	2049	2932	10	80	300	2000	2581	1295
Decrease TA, % planned amounts	25	71	100	100	69	559	20	67	90	100	63	276

TABLE: Plans and downward adjustment in TA, conditional on having plans, by innovator type

Rel.adjustment

FIRMS BY INVESTMENT BEHAVIOR IN R&D

	(1)	(2)
	Invest in R&D continuously	Invest in R&D occasionally
	mean	mean
Invest continuously with budget	0.286	
Invest continuously w/o budget	0.714	
Invest occasionally		0.358
Do not invest typically		0.642
Observations	1818	3672

TABLE: Change of Plans to invest in R&D, BOP-F

Trimmed data; source: Forschungsdaten- und Servicezentrum (FDSZ) der Deutschen Bundesbank, BOP-F, Waves 6-8; trimmed data;

own calculations.

CHANGE IN BUSINESS ACTIVITY IN THE DATA

Average production drop:

- Decrease: 57% of firms, average decrease: 38%.
- Approx. unchanged: 33% of firms.
- Increase: 10% of firms, average decrease: 17%.

ESTIMATION RESULTS: CRISIS EXPOSURE AND INNOVATION CUTS

	Pro	bability to	decrease: F	R&D	Prob	ability to d	ecrease: dif	fusion
	1	2	3	4	5	6	7	8
Crisis-induced production/								
activity drop (0-1)	0.116*** (0.018)	0.092*** (0.019)			0.085*** (0.018)	0.071*** (0.018)		
Crisis-induced production/								
activity drop (pct.)			0.002*** (0.000)	0.001*** (0.000)			0.001*** (0.000)	0.001*** 0.000)
Covariates Observations	No 1317	Yes 1309	No 1186	Yes 1178	No 1295	Yes 1287	No 1163	Yes 1155

Probability to decrease: R&D and technological diffusion. Marginal effects after Heckmann probit. Exclusion criteria is having planned investment in respectively R&D or TD. Report on investments decisions of the firms is collected in the 2021, July-September. Information on recession impact and expectations about next 6 months are collected in June-July 2020.

CHANGE OF PLANS TO INVEST

	(1)	(2)	(3)	(4)
	Planned RD only	Planned TA only	Planned RD and TA	Didnt plan
	mean	mean	mean	mean
No change, RD	0.737	0.986	0.681	0.993
No change, TA	0.984	0.799	0.749	0.992
No change, TA and RD	0.728	0.791	0.620	0.986
Increased, RD	0.079	0.014	0.061	0.007
Increased, TA	0.016	0.039	0.049	0.008
Decreased, RD	0.184		0.258	
Decreased, TA		0.162	0.202	
Observations	380	700	2164	1463

TABLE: Change of Plans to invest, BOP-F

Source: Forschungsdaten- und Servicezentrum (FDSZ) der Deutschen Bundesbank, BOP-F, Waves 6-8, own calculations; trimmed data.

REASONS FOR INCREASE



 $\ensuremath{\mathbf{Figure:}}$ Reasons or firms increasing investments in R&D and TD

DEMAND SHOCK AND SUPPLY CHAIN DISRUPTIONS



Demand-finance

DEMAND SHOCK AND COVID POLICY RESTRICTIONS



Demand-finance

R&D: DISTRIBUTION OF PLANS AND REALIZATION



Notes: Conditional on having plans to invest in R&D

Source: Forschungsdaten- und Servicezentrum (FDSZ) der Deutschen Bundesbank, BOP-F, Waves 6-8, own calculations.

DIFFUSION : DISTRIBUTION OF PLANS AND REALIZATION



Notes: Conditional on having plans to invest in TD.

Source: Forschungsdaten- und Servicezentrum (FDSZ) der Deutschen Bundesbank, BOP-F, Waves 6-8, own calculations.

SHORT-LIVED VS. PERSISTENT CRISES



Magnitude of slowdown in technology growth (V-shape vs. L-shape)

R&D SECTOR: TECHNOLOGICAL FRONTIER

- Growth through expanding varieties
- Innovators invest in R&D to invent new intermediate goods
- Law of motion of technological frontier: $Z_{t+1} = \phi Z_t + \varphi_t X_t$
- Innovator *i*'s production function: $V_t^i = \varphi_t X_t^i = \frac{\chi Z_t}{Z_t^{\zeta} X_t^{1-\zeta}} X_t^i$
- Positive spillover from aggregate innovation stock Z_t , externality from aggregate R&D efforts $(\frac{1}{Z_t^{\zeta} X_t^{1-\zeta}})$, where $0 < \zeta < 1$
- Aggregate R&D: $X_t = \int_i X_t^i di$

ENTREPRENEURS' PROBLEM

Innovator *i* chooses R&D investment X_t^i to maximize:

$$\max_{\left\{X_{t+j}^{i}\right\}_{j=0}^{\infty}} \mathbb{E}_{t} \left\{ \sum_{j=0}^{\infty} \left[\Lambda_{t,t+1+j} J_{t+1+j} \varphi_{t+j} X_{t+j}^{i} - (1+f^{x}) X_{t+j}^{i} \right] \right\}$$

Optimality condition for R&D:

$$\mathbb{E}_t\left(\Lambda_{t,t+1}J_{t+1}\varphi_t\right) = \Delta f^{\mathsf{x}}$$

Aggregate new technologies:

$$V_t = \int_i V_t^i di = \chi Z_t^{1-\zeta} X_t^{\zeta}$$

TECHNOLOGY ADOPTION SECTOR

- Adopters buy right to use unadopted technology from innovators at competitive price J_t
- Technologies are rendered usable in production using equipment E_t^i
- Probability of successful adoption ($\kappa_{\lambda} > 0$, $0 < \eta < 1$, $0 < \rho_{\lambda} < 1$)

$$\lambda_t \left(E_t^i \right) = \kappa_\lambda \left(\frac{X_t}{A_t} \right)^\eta \left(E_t^i \right)^{\rho_\lambda}$$

• Successfully adopted technology is sold at price H_t $H_t = \prod_t + \phi \mathbb{E}_t (\Lambda_{t,t+1} H_{t+1})$

ADOPTERS' PROBLEM

• Adopters weigh adoption costs against the expected gains from technology adoption:

$$J_t = \max_{E_t^i} -Q_t^a E_t^i + \phi \mathbb{E}_t \left\{ \Lambda_{t,t+1} \left[\lambda_t H_{t+1} + (1-\lambda_t) J_{t+1} \right] \right\}$$

• Optimality condition for adoption:

$$\rho_{\lambda}\kappa_{\lambda}\phi\left(\frac{X_{t}}{A_{t}}\right)^{\eta}\mathbb{E}_{t}\left[\Lambda_{t,t+1}\left(H_{t+1}-J_{t+1}\right)\right]=Q_{t}^{a}E_{t}^{1-\rho_{\lambda}}$$

• Law of motion for adopted technologies:

$$A_{t+1} = \phi A_t + \phi \left[\lambda_t \left(Z_t - A_t \right) \right]$$

INTERMEDIATE GOODS PRODUCTION

• Intermediate goods output:
$$Y_t^m = \left[\int_0^{A_t} \left(Y_t^{im}\right)^{\frac{\vartheta-1}{\vartheta}} di\right]^{\frac{\vartheta}{\vartheta-1}}$$

- Price of intermediate good composite: $P_t^m = \left[\int_0^{A_t} \left(P_t^i\right)^{1-\vartheta} di\right]^{\frac{1}{1-\vartheta}}$
- Intermediate good production function: $Y_t^{im} = \theta_t \left(K_t^i\right)^{\alpha} \left(L_t^i\right)^{1-\alpha}$
- Cost minimization:

$$\alpha \frac{\vartheta - 1}{\vartheta} \frac{P_t^m}{P_t} \frac{Y_t^m}{K_t} = R_t^k$$
$$(1 - \alpha) \frac{\vartheta - 1}{\vartheta} P_t^m \frac{Y_t^m}{L_t} = W_t$$

• Aggregation:

$$Y_t = \theta_t A_t^{\frac{1}{\vartheta - 1}} K_t^{\alpha} L_t^{1 - \alpha}$$

FINAL GOOD PRODUCTION

• Final good composite:
$$Y_t = \left[\int_0^1 Y_t^{i\frac{\mu-1}{\mu}di}\right]^{\frac{\mu}{\mu-1}}$$

- Price index of final good: $P_t = \left[\int_0^1 P_t^{i^{1-\mu}} di\right]^{\frac{1}{1-\mu}}$
- Final goods producer *i*'s output:

$$Y_t^i = \left(\frac{P_t^i}{P_t}\right)^{-\mu} Y_t$$

- Price indexation: $P_t^i = P_{t-1}^i \pi_{t-1}^{\iota_p} \bar{\pi}^{1-\iota_p}$
- Final good producer's problem (s.t. equ. 34)

$$\max_{P_{t}^{*}} \mathbb{E}_{t} \sum_{j=0}^{\infty} \xi_{p}^{j} \Lambda_{t,t+j} \left(\frac{P_{t}^{*} \prod_{k=1}^{j} \pi_{t+k-1}^{\iota_{p}} \bar{\pi}^{1-\iota_{p}}}{P_{t+j}} - \frac{P_{t+j}^{m}}{P_{t+j}} \right) Y_{t+j}^{i}$$

CAPITAL PRODUCERS: INVESTMENT

• Capital producers turn final output into capital which they sell to households at price Q_t

$$\mathbb{E}_t \left\{ \sum_{j=0}^{\infty} \Lambda_{t,t+1+j} \left[Q_{t+j} I_{t+j} - (1+f') I_{+j} \right] \right\}$$

• Marginal costs of generating investment goods equals their price:

$$Q_t = 1 + f_i\left(\frac{I_t}{I_{t-1}}\right) + \frac{I_t}{I_{t-1}}f_i'\left(\frac{I_t}{I_{t-1}}\right) - \mathbb{E}_t\left[\Lambda_{t+1}\left(\frac{I_t}{I_{t-1}}\right)^2 f_i'\left(\frac{I_t}{I_{t-1}}\right)\right]$$

• Law of motion of capital:

$$K_{t+1} = (1 - \delta) K_t + I_t$$

EMPLOYMENT AGENCIES

- Continuum of households $i \in [0,1]$ monopolistically supply specialized labor L_t^i
- Large number of competitive employment agencies:

$$L_t = \left[\int_0^1 L_t^{i\frac{\omega-1}{\omega}} di\right]^{\frac{\omega}{\omega-1}}$$

• Labor demand for type *i*:

$$L_t^i = \left(\frac{W_t^i}{W_t}\right)^{-\omega} L_t$$

• Wages:

$$W_t = \left[\int_0^1 W_t^{i^{1-\omega}} di
ight]^{rac{1}{1-\omega}}$$

HOUSEHOLDS

• Household *i* maximizes utility

$$\mathbb{E}_{t}\left\{\sum_{j=0}^{\infty}\beta^{j}\left[\log\left(C_{t+j}-hC_{t+j-1}\right)-\frac{\psi}{1+\nu}L_{i,t+j}^{1+\nu}\right]\right\}$$

subject to the budget constraint

$$\frac{W_t^i}{P_t} L_t^i + R_t \frac{B_t}{P_t} + \left(R_t^k + (1-\delta) Q_t \right) K_t + \Pi_t = C_t + \frac{B_{t+1}}{P_t} + Q_t K_{t+1}$$

• Optimal wage set subject to labor demand:

$$\max_{W_{t}^{*}} \mathbb{E}_{t} \sum_{j=0}^{\infty} \left\{ \left(\xi_{w} \beta \right)^{j} \left[\frac{U_{c,t+j}}{P_{t+j}} L_{t+j}^{i} W_{t}^{*} \prod_{k=1}^{j} \left(1+g \right) \pi_{t+k-1}^{\iota_{w}} \bar{\pi}^{1-\iota_{w}} - \frac{\psi}{1+\nu} \left(L_{t+j}^{i} \right)^{1+\nu} \right] \right\}$$

• Wage indexation: $W^i_t = W^i_{t-1} \left(1 + g
ight) \pi^{\iota_w}_{t-1} ar{\pi}^{1-\iota_w}$

Monetary authority sets policy rate according to:

$$R_t = \left(\left(\frac{\pi_t}{\pi^*} \right)^{\gamma_\pi} \left(\frac{y_t}{y_t^{pot}} \right)^{\gamma_y} R_n \right)^{1-\rho_r} (R_{t-1})^{\rho_r} r_t^m$$

Aggregation

$$Y_t = C_t + f^I I_t + f^X X_t + f^A I_t^A$$

PARAMETERIZATION

Parameter	Description	Value
α	Capital share	0.33
β	Discount factor	0.999
h	Habit persistence	0.50
ν	Inverse Frisch elasticity	0.50
δ	Capital depreciation	0.025
$f_{\mu}^{\prime\prime}$	Capital adjustment costs	5.5
Ĺ	Steady state employment	1
9 _p	Calvo prices	0.93
9w	Calvo wages	0.9
lp	Price indexation	0.5
lw.	Wage indexation	0.5
μ	Elasticity of substitution (final goods)	6
ω	Elasticity of substitution (labor)	6
γ_{π}	Inflation weight	1.5
γ_y	Output weight	1
0r	Persistence (policy rule)	0.8
π*	Inflation target (quarterly)	0.005
9	Elasticity of substitution (intermediates)	2.493
5	R&D elasticity	0.304
ρ^{λ}	Adoption elasticity	0.925
$\bar{\lambda}$	Steady state adoption rate	0.05
η	R&D-adoption spillover	0.294
$1 - \phi$	Obsolescence rate	0.025
f"	Adjustment costs R&D	6
$f_{ta}^{\prime\prime}$	Adjustment costs adoption	6
$100 * (\bar{g}^{\frac{1}{\vartheta - 1}})$	Technology growth (steady state)	0.5