Do Higher Interest Rates Make The Banking System Safer? Evidence From Bank Leverage

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Bank of Finland and CEPR Joint Conference 2024 Back to Basics and Beyond: New Insights for Monetary Policy Normalisation

Paul Samuelson (AER, 1945)

"Simple truths need constant repetition...

- 1. The banking system as a whole is not really hurt by an increase in the whole complex of interest rates. It is left tremendously better off by such a change.
- 2. A typical single bank, taken by itself, is not really hurt by an increase in the whole complex of interest rates. It is left better off by such a change."

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Janet Yellen (2014)

"that low interest rates contribute to increased leverage and reliance on short-term funding points toward some ability of higher interest rates to lessen these vulnerabilities"

Vast theoretical literature predicts contractionary monetary policy makes banks safer through *reducing* bank leverage.

Theoretical predictions

- (i) Van der Ghote (AEJ:Macro, 2021) / Martin, Medicino, Van der Ghote (ECB DP, 2021) "This is true in most models ... By tightening ex ante, monetary policy contributes to reducing credit and, more specifically, leverage"
- (ii) Martinez-Miera & Repullo (ARE, 2021) (extending MMR (ECMA, 2017))
 "Such [monetary] tightening reduces aggregate investment . . . and reduces bank leverage and risk-taking"
- (iii) Drechsler, Savov, Schnabl (JF, 2018)

"Lower nominal rates make liquidity cheaper and raise leverage"

(iv) Dell'Ariccia, Laeven, Marquez (JET, 2014)

"We obtain two main findings. First, a reduction in risk-free interest rates leads banks to increase their leverage."

(v) Angeloni and Faia (JME, 2013)

"The increase in interest rate activates the risk taking channel: bank leverage and risk decline"

(vi) Woodford (NBER WP, 2012)

"It is appropriate to use monetary policy to 'lean against' a credit boom, even if this requires both inflation and the output gap to be below their medium-run target values for a time."

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Empirics

Limited empirical evidence & minimal discussion of core mechanisms.

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Why this matters

- I. Positive: How does monetary policy transmit through banks?
- II. Normative: Should monetary policy target financial stability?



- (i) Empirically, how do monetary policy shocks affect bank leverage?
- (ii) What mechanism can explain this?

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- (ii) Empirical evidence of a loan-loss mechanism: MP shock \Rightarrow loan losses $\uparrow \Rightarrow$ profit $\downarrow \Rightarrow$ bank equity $\downarrow \Rightarrow$ leverage \uparrow

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- (iv) Evidence from micro data consistent with role of floating-rate loans

For h = 0, ..., H, I estimate the following series of Jordà local projections using FDIC quarterly data between 1984 and 2006:

$$z_{t+h} = \alpha_h + \sum_{l=0}^{L} \beta_{h,l} Shock_{t-l} + \sum_{m=1}^{M} \gamma_{h,m} z_{t-m} + \sum_{q=2}^{4} \delta_q Quarter_{qt} + \epsilon_{t+h}$$
(1)

• z_{t+h} : variable of interest (e.g., leverage).

- Shock_{t-l}: monetary policy shock series
- · z_{t-m} : lag-augmentation (see Montiel Olea & Plagborg-Møller (ECMA, 2021)).
- Baseline horizon and lags: H = L = M = 16
- IRF is sequence $\{\beta_{h,0}\}_{h=0}^{H}$ which captures the response of *z* at time t + h to *Shock* at time *t*.
- Robustness checks: use alt. definition of leverage, vary lags, include time trends, vary sample periods, and use different MP shock series.

The Response of Bank Leverage



68% and 90% confidence bands displayed

Definition Time Periods Lags Shocks Market L

Contractionary Shock

 \Rightarrow Leverage \uparrow

Contractionary Shock

 \Rightarrow Loans Passed Due \uparrow

 \Rightarrow Loan Losses \uparrow

 \Rightarrow Profits \downarrow

 \Rightarrow Book Equity \downarrow

 \Rightarrow Leverage \uparrow









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How important is my mechanism?

- 1. loan-losses $\uparrow \Rightarrow \text{profit} \downarrow$
- 2. profit $\downarrow \Rightarrow$ leverage \uparrow

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1. loan-losses $\uparrow \Rightarrow \text{profit} \downarrow$

By how much?

2. profit $\downarrow \Rightarrow$ leverage \uparrow

1. Loan-Losses to Profits

Net Interest Income	Net Noninterest Income	Other Income	Provisions	Profits
Assets	Assets	Assets	Assets	Assets

1. Loan-Losses to Profits

Profits (excluding provisions)

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2. Profits to Leverage

Cumulative Profits	Cumulative Dividends	$_{\sim}$ Equity _	1
Assets	Assets	\sim Assets	Leverage

2. Profits to Leverage

 $\frac{\text{Cumulative Profits}}{\text{Assets}} - \frac{\text{Cumulative Dividends}}{\text{Assets}} \approx \frac{\text{Equity}}{\text{Assets}} = \frac{1}{\text{Leverage}}$



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- 2. profit $\downarrow \Rightarrow$ leverage \uparrow

 \Rightarrow My mechanism explains most of the response of leverage

 \checkmark

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 \Rightarrow But why do contractionary MP shocks increase loan losses?

Two potential reasons for loan losses:

- (1) ↑ FFR: higher costs on floating-rate (or short-term fixed-rate) loans reduces ability to repay
- (2) \downarrow GDP: lower borrower income reduces ability to repay

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Empirical Test: If loan losses only respond to MP shock, then floating-rate loans are likely an important channel.

Suggestive driver of loan losses



Romer-Romer

Oil Shock



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$\Rightarrow \uparrow$ FFR is important: potential role for floating-rate loans

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 - \Rightarrow Issuing floating-rate loans hedges interest rate risk but generates credit risk
- \Rightarrow Key tension in the model when interest rates rise:
 - (A) Higher net interest income due to floating-rate loans (↑ profits)
 - (B) Higher loan losses due to loan-loss mechanism (\downarrow profits)
 - $\Rightarrow\,$ Net impact on profits (and subsequently leverage) depends on (A) vs (B)



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Specification:

I use bank-level variation in floating shares from 1997 to 2006 to estimate panel local projections:

$$\begin{aligned} Z_{i,t+h} &= \alpha_{i,h} + \sum_{l=0}^{L} \beta_{h,l}^{(1)} Shock_{t-l} + \beta_{h}^{(2)} FloatShare_{i,t} + \sum_{l=0}^{L} \beta_{h,l}^{(3)} Shock_{t-l} \cdot FloatShare_{i,t} \\ &+ \sum_{m=1}^{M} \gamma_{h,m} Z_{t-m} + \sum_{q=2}^{4} \delta_{q} Quarter_{qt} + \epsilon_{i,t+h} \end{aligned}$$

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Model Prediction:

 $\{\beta_{h,0}^{(3)}\}_{h=0}^{H}$ and $\{\beta_{h,0}^{(1)} + \beta_{h,0}^{(3)} \cdot FloatShare_{i,t}\}_{h=0}^{H}$ for h = 0...16 show that in response to a MP shock, a bank with a higher floating share should:

- 1. Have higher net interest income (less interest rate risk)
- 2. Have higher provisions (more credit risk)

Net Interest Income Impulse Response Functions



Loan-Loss Provisions Impulse Response Functions



Profits Impulse Response Functions



Conclusion

Contributions

- 1. Show that contractionary MP shocks increase bank leverage
- 2. Propose and empirically validate a mechanism that can explain this result: the loan-loss mechanism
- 3. Develop a different way of modelling banks that explains this mechanism through risk transformation and floating-rate loans
- 4. Show that empirical evidence using micro data is consistent with the role of floating-rate loans in the model

Conclusion

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- 1. Show that contractionary MP shocks increase bank leverage
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Take-away

- ⇒ Contractionary monetary policy can have unintended consequences for bank vulnerability through floating-rate loans
- ⇒ If the goal is to reduce bank leverage, use macroprudential policy and let monetary policy focus on price stability

Definition

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Why do we care?

- Externalities (e.g., fire-sales, moral hazard)
- Propagation and amplification of shocks (financial accelerator)
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Post-Crisis Response

- (i) Policy: Regulations across the world restricting bank leverage
- (ii) Research: Rush to build models which incorporate financial frictions

Different Definition of Leverage



68% and 90% confidence bands displayed

Different Time Periods



Different Lag Lengths



Different Shock Series (1994-2006)



68% and 90% confidence bands displayed

Market Leverage with Different Shock Series (1994-2006)



68% and 90% confidence bands displayed

Decomposition of leverage response



Provisions and Write-Offs



68% and 90% confidence bands displayed

Back

Share of Floating-Rate Loans in the Time Series & Cross Section



Cross-Sectional Variation

Monetary Policy Shocks versus Changes in the Fed Funds Rate



Back

Woodford (2012)

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\Rightarrow Implicit assumption: higher interest rates reduce bank vulnerability

- One period model with the following timing:
 - 1. Beginning: banks make loans funded by deposits and net worth
 - 2. Middle: shock realisation
 - 3. End: Settlement takes place
- Banks are exogenously endowed with deposits *D*, a loan portfolio of size *L*. Internal net worth N = L - D.
- The key choice of the bank is the share of floating-rate loans f_L .
- Deposits are floating-rate liabilities with imperfect pass-through 0 $<\beta^{dep}<$ 1 which is exogenous.
- The interest rate is a random variable $r = \overline{r} + \varepsilon$ where $\varepsilon \sim \mathcal{N}(0, \sigma^2)$. So, $E[r] = \overline{r}, Var[r] = \sigma^2$. Note that ε is a 'shock' to interest rates.
- $\theta(\varepsilon)$ is the loan-loss rate. $\theta'(\varepsilon) > 0$ and $\theta'(\varepsilon)$ is linear in ε .

• The bank objective is to maximise value by choosing the share of its loans that are floating-rate

$$\max_{f_L} V = E[\pi] - \frac{\gamma}{2} Var[\pi]$$

where π represents bank profits and γ represents risk-aversion.

• Solving the bank problem yields an optimal choice of f_L^* .

Bank Solution Firm Solution Equilibrium

Given a bank's optimal choice f_L^* , profits are



where μ^* is the equilibrium loan spread.

Assumption: no loan losses on fixed-rate loans as MP shocks do not affect their loan-servicing costs

- Empirical evidence suggests that floating-rate loans are a potential driver of loan losses in response to MP shocks
- Model focuses on loan losses through floating-rate loans to highlight risk transformation

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- Empirical evidence suggests that floating-rate loans are a potential driver of loan losses in response to MP shocks
- Model focuses on loan losses through floating-rate loans to highlight risk transformation
- \Rightarrow So what are the implications of issuing floating-rate loans?

Define deviations from equilibrium profitability (Return on Assets) as:

$$\Delta \equiv \frac{\pi}{L} - \frac{E[\pi]}{L}$$

$$\implies \Delta = \underbrace{f_L^* \varepsilon - \frac{D}{L} \beta^{dep} \varepsilon}_{\text{interest rate risk}} - \underbrace{f_L^* \left(\theta(\varepsilon) - E[\theta(\varepsilon)]\right)}_{\text{credit risk}}$$

Intuition

- 1. Banks have floating-rate liabilities which expose them to rate risk
- 2. To hedge this risk, banks issue floating-rate loans
- 3. Interest rate risk is passed onto borrowers
- 4. If borrowers cannot hedge this risk, it becomes a credit risk for banks
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 \Rightarrow Banks do risk transformation: interest rate risk becomes credit risk

Differentiating Δ wrt to an interest rate shock allows us to construct the model IRFs as functions of the floating share (f_L):



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In response to MP shock, a bank with a higher floating share (f_L) should:

- 1. Have higher net interest income
 - \Rightarrow Banks with higher f_L are less exposed to interest rate risk
- 2. Have higher loan-loss provisions
 - \Rightarrow Banks with higher f_L are more exposed to credit risk
- \Rightarrow Net impact on profits depends on which dominates

Bank Solution

The bank has the following objective

$$\max_{f_L} V_b = E[\pi_b] - \frac{\gamma}{2} Var[\pi_b]$$

where profits are given by the following

$$\pi_b = L(1 - f_L)(\bar{r} + \mu(f_L)) + Lf_L(\bar{r} + \varepsilon + \mu(f_L)) - D(\bar{r} + \beta\varepsilon) - Lf_L\theta(\varepsilon)$$

Taking the first-order condition with respect to f_L and simplifying yields the following expression for f_l^*

$$f_{L}^{*} = \frac{\frac{\partial \mu(f_{L})}{\partial f_{L}} - \overline{\theta(\varepsilon)}}{\gamma L\left(\sigma_{\varepsilon}^{2} + \sigma_{\theta}^{2} - 2\rho_{\varepsilon\theta}\right)} + \frac{D\beta\left(\sigma_{\varepsilon}^{2} - \rho_{\varepsilon\theta}\right)}{L\left(\sigma_{\varepsilon}^{2} + \sigma_{\theta}^{2} - 2\rho_{\varepsilon\theta}\right)}$$

Firm Solution

The bank has the following objective

$$\max_{l} V_{f} = E[\pi_{f}] - \frac{\gamma}{2} Var[\pi_{f}]$$

where profits are given by the following

 $\pi_f = AI - I - I(1 - f_L)(\overline{r} + \mu(f_L)) - If_L(\overline{r} + \varepsilon + \mu(f_L)) - If_L\theta(\varepsilon)$

Taking the first-order condition with respect to *I* and simplifying yields the following expression for $\mu(f_L)$

$$\mu(f_L) = A - 1 - \bar{r} - f_L \overline{\theta(\varepsilon)} - \gamma l f_L^2 \sigma_{\varepsilon}^2 - \gamma l f_L^2 \sigma_{\theta}^2 - \gamma f_L \rho_{\varepsilon\theta}$$

In equilibrium, we will have a loan spread, μ^* that will equate firm credit demand, *I*, with bank loan size, *L*.

Taking the derivative of μ with respect to f_L^* allows us to obtain a solution for f_l^* in terms of exogenous components

$$f_{L}^{*} = \frac{D\beta\gamma\left(\sigma_{\varepsilon}^{2} - \rho_{\varepsilon\theta}\right) - \gamma\rho_{\varepsilon\theta} - 2\overline{\theta(\varepsilon)}}{\gamma L\left(3\sigma_{\varepsilon}^{2} + 3\sigma_{\theta}^{2} - 2\rho_{\varepsilon\theta}\right)}$$

Back